STUDY ON SOLAR RADIATION OF SURFACE OF THE PHOTOVOLTAIC SYSTEM

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INTRODUCTION

World energy demand is projected to increase by up to 71% between 2003 and 2030 [1]. At present, most of the used energy is generated from the fossil fuels, and despite notable advances in renewable energy technology, it is questionable whether such a demand trajectory can be met in an environmentally sustainable manner [2]. It has been proposed, then, that the one way to reduce burden on fossil fuels is utilize the solar energy through photovoltaic route.

The power produced by the solar photovoltaic module is maximum when module surface is perpendicular to the incident radiation this means the power generated by the PV module not only depends on the intensity of solar radiation but also on slope of the surface i.e. the angle between module and the sun[3-14]. Therefore, set of empirical relation is required for evaluating the amount of solar radiation incident on a tilted surface if the solar radiation on horizontal surface is available. In this paper, a model based on the empirical relations is used for calculating the availability of solar radiation on tilted surface for power generation. A set of readings of the radiation available on horizontal surface is used for the further analysis.

MATHEMATICAL MODEL

Solar flux striking a collector will be a combination of direct beam radiation, scattered or diffused radiation and reflected radiation. Since measurements of solar radiation are often not available, attempts have been made by many hours, cloud cover and precipitation. These equations for solar radiation at a site can be estimated if the latitude, longitude and altitude of location is known. The main aim of this article is to estimate the radiation available on the tilted PV system for power generation. The amount of radiation falling on the tilted surface can be estimated by the following equation [3]:

\[
\frac{I_t}{I_g} = \{1 - \left(\frac{I_d}{I_g}\right)\} \times r_b + \left(\frac{I_d}{I_g}\right) \times r_d \times \rho' r_t
\]

Where, \( I_t \) is total radiation on the tilted surface, \( \rho' \) is reflectivity of ground surface and \( I_g, I_b, I_d \) are hourly global radiation, hourly beam radiation and hourly diffuse radiation respectively.

The radiation shape factor for a tilted surface with respect to sky \( r_d \) and radiation shape factor for the surface with respect to surrounding ground \( r_t \) can be expressed as follows[3]:

\[
r_d = \frac{1 + \cos \beta}{2}
\]

\[
r_t = \frac{1 - \cos \beta}{2}
\]

where, \( \beta \) is tilt angle, \( r_b \) is the ratio of beam radiation flux falling on tilted surface to that falling on horizontal surface, also known tilt factor and it can be expressed by:

\[
r_b = \cos \theta / \cos \theta_z
\]

where, \( \theta \) and \( \theta_z \) are incident and zenith angles, as represented in Figure 1, of the sun ray with surfaces. These angles can be calculated by using the following relations:

\[
\cos \theta = \sin \phi \sin \delta \cos \beta + \cos \delta \cos \gamma \cos \omega \sin \phi \\
\sin \beta + \cos \phi \cos \delta \cos \omega \cos \beta - \cos \phi \cos \gamma \sin \delta
\]

Abstract:

This paper is a mathematical study for finding the amount of solar radiation on the surface of the Photovoltaic (PV) system affected due to the variation in the slope (tilt angle) of the PV system along with the background theory of the attenuation of the solar radiation. The power density is maximum when the solar module-absorbing surface is perpendicular to the sun and in all other cases module power is always lesser than the incident power. Hence extra addition of panels with fixed tilt is no longer economical viable when electricity demand increases. Theoretical estimation of solar radiation on the slope of the PV surface from the radiation available on the horizontal surface is evaluated and the results are presented on the basis of the data available and proposed mathematical model for the calculation of the total amount of solar radiation on tilted surface.

Keywords — Solar Energy, Solar Radiation, Solar Photovoltaic, PV, Solar, solar tilt..
\[
\sin \beta + \cos \delta \sin \gamma \sin \omega \sin \beta 
\]
(5)
for surface facing south \(\gamma = 0^\circ\)
\[
\cos \theta = \sin \delta \sin (\phi - \beta ) + (\cos \delta \cos \omega \cos (\phi - \beta))
\]
(6)
for horizontal surface
\[
\cos \theta_z = \sin \phi \sin \delta + \cos \phi \cos \delta \cos \omega 
\]
(7)
where, \(\phi, \delta, \gamma\) and \(\omega\) are latitude, declination, surface azimuth and hour angles.
\(\gamma\) = Azimuth or the orientation angle of the surface (i.e. the angle between the projection of the normal to the surface on the horizontal plane and the local medium; surface facing south \(\gamma = 0^\circ\), east +, west -).
The hour angle (i.e., each hour equal to \(15^\circ\) of latitude; solar noon is zero, morning +, afternoon -) and can be calculated as:
\[
\omega = (t -12) \times 15
\]
(8)
where \(t\) = solar time
The declination angle can be estimated as follows:
\[
\delta = 23.45 \sin \left( \frac{360}{365}\times(284+N) \right)
\]
(9)
where, \(N\) are No. of days

RESULTS AND DISCUSSION
The values of declination calculated by the above relation are shown in the following figure

Figure 1. Representation of solar angles

Figure 2: Declination angle vs. date

The values of global and diffuse solar radiations and ambient temperature were measured experimentally for various days of the year. The measured values of these parameters are depicted in the Table 1.
The measured values of global and diffuse components of radiation were used to calculate the radiation values for different tilt angle. The model is used for calculating the radiation values for different tilt surfaces. The variation of solar radiation for different tilt angle are depicted in the Figures 3-10.

Figure 3. The amount of radiation incident on the surface of the PV system with 2.2 Deg and 7.7 Deg of tilt for the same horizontal radiation data on Dec 19, 2008.

Figure 4. The amount of radiation incident on the surface of the PV system with 2.7 Deg and 7.7 Deg of tilt for the same horizontal radiation data on Dec 23, 2008.
Figure 5. The amount of radiation incident on the surface of the PV system with 12.7 Deg and 17.7 Deg of tilt for the same horizontal radiation data on Dec 15, 2008.

Figure 6. The amount of radiation incident on the surface of the PV system with 12.7 Deg and 17.7 Deg of tilt for the same horizontal radiation data on Dec 17, 2008.

Figure 7. The amount of radiation incident on the surface of the PV system with 22.7 Deg and 27.7 Deg of tilt for the same horizontal radiation data on Dec 24, 2008.

Figure 8. The amount of radiation incident on the surface of the PV system with 22.7 Deg and 27.7 Deg of tilt for the same horizontal radiation data on Dec 27, 2008.

Figure 9. The amount of radiation incident on the surface of the PV system with 32.7 Deg and 37.7 Deg of tilt for the same horizontal radiation data on Dec 29, 2008.
Figure 10. The amount of radiation incident on the surface of the PV system with 32.7 Deg and 37.7 Deg of tilt for the same horizontal radiation data on Dec 30, 2008.

Table2. showing the conversion efficiency of the PV system with the amount of Short circuit current generated with the solar radiation falling on the tilted PV surface

<table>
<thead>
<tr>
<th>Tilt Angle</th>
<th>Amount of Total Radiation Incident (W/m²)</th>
<th>Amount of Total Short Circuit Current Generated (A)</th>
<th>Conversion Efficiency</th>
</tr>
</thead>
<tbody>
<tr>
<td>Latitude -20</td>
<td>4806</td>
<td>25.25</td>
<td>5.25 * 10⁻³</td>
</tr>
<tr>
<td>Latitude -15</td>
<td>4806</td>
<td>27.66</td>
<td>5.75* 10⁻³</td>
</tr>
<tr>
<td>Latitude -10</td>
<td>5760</td>
<td>36.56</td>
<td>6.35 * 10⁻³</td>
</tr>
<tr>
<td>Latitude -5</td>
<td>6330</td>
<td>41.29</td>
<td>6.52 * 10⁻³</td>
</tr>
<tr>
<td>Latitude</td>
<td>8612</td>
<td>59.88</td>
<td>6.95 * 10⁻³</td>
</tr>
<tr>
<td>Latitude +5</td>
<td>8612</td>
<td>62.87</td>
<td>7.3 * 10⁻³</td>
</tr>
<tr>
<td>Latitude +10</td>
<td>7764</td>
<td>56.2</td>
<td>7.24 * 10⁻³</td>
</tr>
</tbody>
</table>

The proposed model is quite successful in finding the incident solar radiation on tilted surface when horizontal data for radiation is available. Also the graphical representation shows the amount of variation in solar radiation incident on the surface of PV system i.e. variation in solar radiation intensity with the slope of the PV system with respect of horizontal. The mathematical model is useful in order to evaluate the total amount of solar radiation on tilted surface when the radiations on horizontal surfaces are known. The calculated results obtained here are used for finding the optimization of tilt angle for Photovoltaic system and presented.[13] and is represented in above Table2 hence it verify Results are evaluated and verified by the comparison in the graph for different tilt angle on the same day and location.

CONCLUSION

Mathematical model is quite helpful to illustrate and estimate the general trends of the distribution of solar energy which varies with geographical location, altitude, and the time of the year and also by local weather condition. It can be concluded from the results that the PV module should be optimally inclined to obtain the maximum power output. The inclination angle may vary location to location and day to day.

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